

### Overview of Session 10

- Analyzing and narrating a fraction-of-a-set task
- Identifying teaching moves that support the class in understanding representations shared by classmates
- Summarizing teaching moves that support students in understanding representations shared by classmates

### Supporting and using student representations

This teaching practice:

- Scaffolds student opportunities to engage in a crucial mathematical practice
- Provides the teacher with examples of student thinking
- Models interest in the thinking of others
- Helps the class to make sense of the ideas and their relationship to the mathematics of the lesson

2

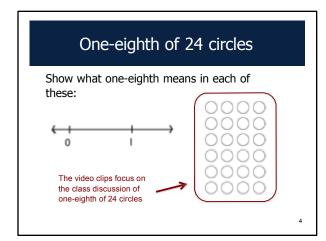
# Video clips from a fifth-grade lesson on fractions

- Entering 5<sup>th</sup> graders (10 year-olds)
- Two week summer program (7<sup>th</sup> class session out of 10)
   The class generated, and had been refining over several class sessions, a working definition of a "fraction"
  - They had been examining fractions with
    - Drawings (rectangles, circles)
    - Cuisenaire rods
    - Sets of objects as the whole
    - Number line
- They had started mapping one representation onto others
  Students came with a wide range of mathematical skills
  - and varying degrees of interest in mathematics

3

This work is licensed under a Creative Commons Attribution-Noncommercial-4.0 International License: https://creativecommons.org/licenses/by-nc/4.0/ © 2018 Mathematics Teaching and Learning to Teach School of Education • University of Michigan • Ann Arbor, MI 48109-1259 • mtlt@umich.edu

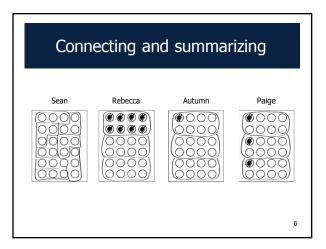






#### Focus questions

- What does the teacher do to support the students' recording?
- What does she ask as the students record? What purpose might the teacher have for those prompts?
- How does the teacher use another student's thinking to help the class make sense of the mathematics?





This work is licensed under a Creative Commons Attribution-Noncommercial-4.0 International License: https://creativecommons.org/licenses/by-nc/4.0/ © 2018 Mathematics Teaching and Learning to Teach School of Education • University of Michigan • Ann Arbor, MI 48109-1259 • mtlt@umich.edu

5



# Making connections with representations

- Between student(s) thinking and a representation
   Explanation related to a particular aspect of a diagram
- Within representations of the same type
   Rectangular area models
   Assess representations of the same type
- Across representations of the same type
   Rectangular area and circular area
- Across representations of different types
   Across representations of different types
   Across representations of different types
- Between representation and the problem statement
   Checking on the correspondence of what a problem asks and features of a representation
- Connecting mathematical language and ideas to representations

   Using subject matter terminology and ideas to name and describe aspects of representations

#### Focus questions

- What connections does the teacher make in the summary?
- What key mathematical points are made?
- What purposes do those connections and key points seem to serve?

# Supporting the class in understanding making use of representations shared by classmates

What is the work of teaching?

- Requesting recording (to capture a method/way of thinking, clarify something that is unclear)
- Probing student thinking in relation to what is recorded and the mathematics of the task
- Restating student thinking and checking on its accuracy
- Connecting representations
- Inviting comments/thinking from the class
- Summarizing status or progress of the work

9

8

This work is licensed under a Creative Commons Attribution-Noncommercial-4.0 International License: https://creativecommons.org/licenses/by-nc/4.0/ © 2018 Mathematics Teaching and Learning to Teach School of Education • University of Michigan • Ann Arbor, MI 48109-1259 • mtlt@umich.edu



#### Module summary

What are you taking from this module in terms of:

- Mathematical ideas
- Definition of fractions, representations of fractions, comparing, and equivalence
- Using representations in teaching
   Onnecting, narrating, using public recording space
- Student thinking about fractions

   Strategies, ways of explaining and representing
- Ways of learning from your teaching
   Studying records of your use of public recording space

10